

# Course 395: Machine Learning

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- Lecturers: Maja Pantic (maja@doc.ic.ac.uk)  
Stavros Petridis (sp104@doc.ic.ac.uk)
- Goal (Lectures): To present basic theoretical concepts and key algorithms that form the core of machine learning
- Goal (CBC): To enable hands-on experience with implementing machine learning algorithms (developed using Matlab or Python)
- Material: *Machine Learning* by Tom Mitchell (1997)  
*Neural Networks & Deep Learning* by Michael Nielsen (2017)  
Manual for completing the CBC
- More Info: <https://www.ibug.doc.ic.ac.uk/courses>

# Course 395: Machine Learning – Lectures

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- Lecture 1-2: Concept Learning (*M. Pantic*)
- Lecture 3-4: Decision Trees & CBC Intro (*M. Pantic & S. Petridis*)
- Lecture 5-6: Evaluating Hypotheses (*S. Petridis*)
- Lecture 7-8: Artificial Neural Networks I (*S. Petridis*)
- Lecture 9-10: Artificial Neural Networks II (*S. Petridis*)
- Lecture 11-12: Artificial Neural Networks III (*S. Petridis*)
- Lecture 13-14: : Instance Based Learning & Genetic Algorithms (*M. Pantic*)

# Course 395: Machine Learning - CBC

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- Lecture 1-2: Concept Learning
- Lecture 3-4: Decision Trees & **CBC Intro**
- Lecture 5-6: Evaluating Hypotheses
- Lecture 7-8: Artificial Neural Networks I
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- Lecture 13-14: Instance Based Learning & Genetic Algorithms

# Course 395: Machine Learning

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## NOTE

*CBC accounts for 33.3% of the final grade for the Machine Learning Exam.*

$$final\_grade = \frac{2}{3} exam\_grade + \frac{1}{3} exam\_grade$$

# Course 395: Machine Learning – Lectures

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## ➤ Lecture 1-2: Concept Learning

- Lecture 3-4: Decision Trees & CBC Intro
- Lecture 5-6: Evaluating Hypotheses
- Lecture 7-8: Artificial Neural Networks I
- Lecture 9-10: Artificial Neural Networks II
- Lecture 11-12: Artificial Neural Networks III
- Lecture 13-14: Instance Based Learning & Genetic Algorithms

# Concept Learning – Lecture Overview

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- Why machine learning?
- Well-posed learning problems
- Designing a machine learning system
- Concept learning task
- Concept learning as Search
- Find-S algorithm
- Candidate-Elimination algorithm

# Machine Learning

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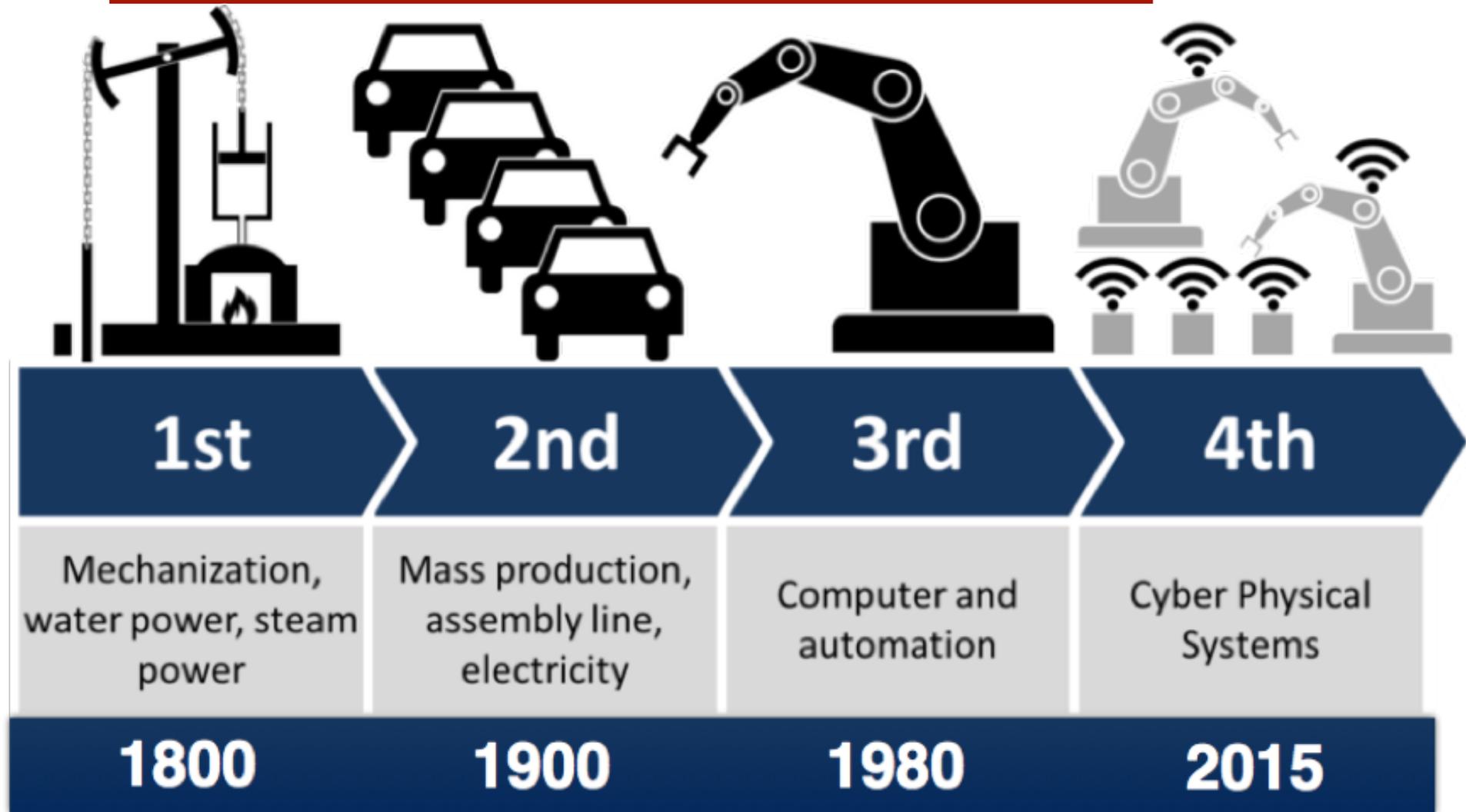
- Learning  $\leftrightarrow$  Intelligence  
(Def: *Intelligence is the ability to learn and use concepts to solve problems.*)
- Machine Learning  $\leftrightarrow$  Artificial Intelligence
  - Def: *AI is the science of making machines do things that require intelligence if done by men* (Minsky 1986)
  - Def: *Machine Learning is an area of AI concerned with development of techniques which allow machines to learn*
- Why Machine Learning?  $\leftrightarrow$  Why Artificial Intelligence?

# Machine Learning

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# Machine Learning



# Machine Learning

NEURAL COMMUNICATION

WORLD ECONOMIC FORUM

We'll **control** gadgets with **brain signals**

The world will be one in which we can **communicate** our intent **directly and instantly** to machines and have very **complex outcomes**

# Machine Learning

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- Learning  $\leftrightarrow$  Intelligence  
(Def: *Intelligence is the ability to learn and use concepts to solve problems.*)
- Machine Learning  $\leftrightarrow$  Artificial Intelligence
  - Def: *AI is the science of making machines do things that require intelligence if done by men* (Minsky 1986)
  - Def: *Machine Learning is an area of AI concerned with development of techniques which allow machines to learn*
- Why Machine Learning?  $\leftrightarrow$  Why Artificial Intelligence?
  - $\equiv$  To build machines exhibiting intelligent behaviour (i.e., able to reason, predict, and adapt) while helping humans work, study, and entertain themselves

# Machine Learning

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- Machine Learning  $\leftrightarrow$  Artificial Intelligence
- Machine Learning  $\leftarrow$  Biology (e.g., Neural Networks, Genetic Algorithms)
- Machine Learning  $\leftarrow$  Cognitive Sciences (e.g., Case-based Reasoning)
- Machine Learning  $\leftarrow$  Statistics (e.g., Support Vector Machines)
- Machine Learning  $\leftarrow$  Probability Theory (e.g., Bayesian Networks)
- Machine Learning  $\leftarrow$  Logic (e.g., Inductive Logic Programming)
- Machine Learning  $\leftarrow$  Information Theory (e.g., used by Decision Trees)

# Machine Learning

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- Human Learning  $\leftrightarrow$  Machine Learning
  - human-logic inspired problem solvers (e.g., rule-based reasoning)
  - biologically inspired problem solvers (e.g., Neural Networks)
    - supervised learning - generates a function that maps inputs to desired outputs
    - unsupervised learning - models a set of inputs, labelled examples are not available
  - learning by education (e.g., reinforcement learning, case-based reasoning)
- General Problem Solvers vs. Purposeful Problem Solvers
  - emulating general-purpose human-like problem solving is impractical
  - restricting the problem domain results in ‘rational’ problem solving
  - example of General Problem Solver: Turing Test
  - examples of Purposeful Problem Solvers: speech recognisers, face recognisers, facial expression recognisers, data mining, games, etc.
- Application domains: security, medicine, education, finances, genetics, etc.

# Well-posed Learning Problems

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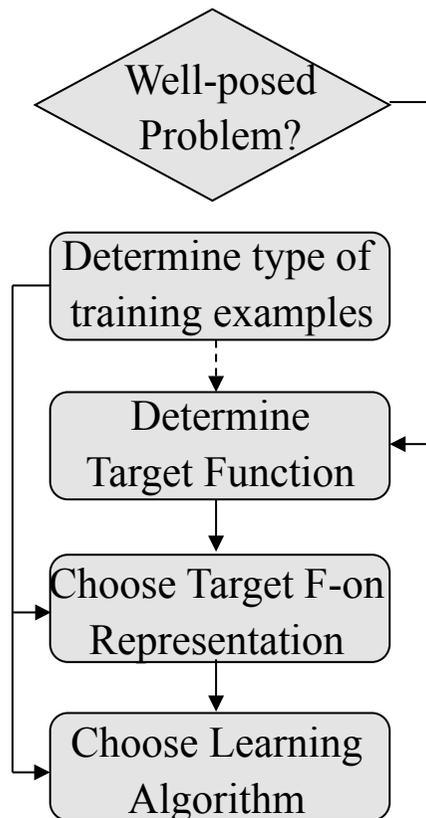
- Def 1 (*Mitchell 1997*):

*A computer program is said to learn from experience  $E$  with respect to some class of tasks  $T$  and performance measure  $P$ , if its performance at tasks in  $T$ , as measured by  $P$ , improves by experience  $E$ .*

- Def 2 (*Hadamard 1902*):

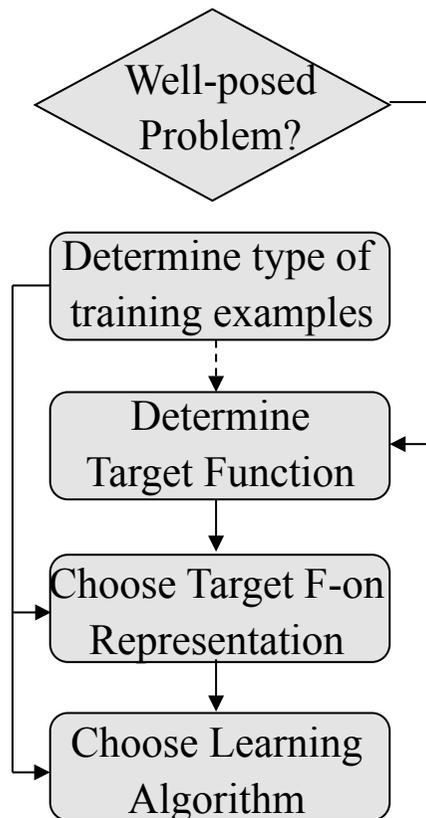
*A (machine learning) problem is well-posed if a solution to it exists, if that solution is unique, and if that solution depends on the data / experience but it is not sensitive to (reasonably small) changes in the data / experience.*

# Designing a Machine Learning System



- Target Function  $V$  represents the problem to be solved (e.g., choosing the best next move in chess, identifying people, classifying facial expressions into emotion categories)
- $V: D \rightarrow C$  where  $D$  is the input state space and  $C$  is the set of classes  
 $V: D \rightarrow [-1, 1]$  is a general target function of a binary classifier
- Ideal Target Function is usually not known; machine learning algorithms learn an approximation of  $V$ , say  $V'$
- Representation of function  $V'$  to be learned should
  - be as close an approximation of  $V$  as possible
  - require (reasonably) small amount of training data to be learned
- $V'(d) = w_0 + w_1x_1 + \dots + w_nx_n$  where  $\langle x_1 \dots x_n \rangle \equiv d \in D$  is an input state. This reduces the problem to learning (the most optimal) weights  $w$ .

# Designing a Machine Learning System



- $V: D \rightarrow C$  where  $D$  is the input state and  $C$  is the set of classes  
 $V: D \rightarrow [-1, 1]$  is a general target function of a binary classifier
- $V'(d) = w_0 + w_1x_1 + \dots + w_nx_n$  where  $\langle x_1 \dots x_n \rangle \equiv d \in D$  is an input state. This reduces the problem to learning (the most optimal) weights  $w$ .
- Training examples suitable for the given target function representation  $V'$  are pairs  $\langle d, c \rangle$  where  $c \in C$  is the desired output (classification) of the input state  $d \in D$ .
- Learning algorithm learns the most optimal set of weights  $w$  (so-called *best hypothesis*), i.e., the set of weights that best fit the training examples  $\langle d, c \rangle$ .
- Learning algorithm is selected based on the availability of training examples (supervised vs. unsupervised), knowledge of the final set of classes  $C$  (offline vs. online, i.e., eager vs. lazy), availability of a tutor (reinforcement learning).
- The learned  $V'$  is then used to solve new instances of the problem.

# Concept Learning

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- Concept learning
  - supervised, eager learning
  - target problem: whether something belongs to the target concept or not
  - target function:  $V: D \rightarrow \{\text{true}, \text{false}\}$
- Underlying idea: Humans acquire general concepts from specific examples (e.g., concepts: beauty, good friend, well-fitting-shoes)  
(note: each concept can be thought of as Boolean-valued function)
- Concept learning is inferring a Boolean-valued function from training data  
→ concept learning is the prototype binary classification

# Concept Learning Task – Notation

- Concept learning task:
  - target concept: Girls who Simon likes
  - target function:  $c: D \rightarrow \{0, 1\}$
  - data  $d \in D$ : Girls, each described in terms of the following attributes
    - $a_1 \equiv \text{Hair}$  (possible values: blond, brown, black)
    - $a_2 \equiv \text{Body}$  (possible values: thin, average, plump)
    - $a_3 \equiv \text{likesSimon}$  (possible values: yes, no)
    - $a_4 \equiv \text{Pose}$  (possible values: arrogant, natural, goofy)
    - $a_5 \equiv \text{Smile}$  (possible values: none, pleasant, toothy)
    - $a_6 \equiv \text{Smart}$  (possible values: yes, no)
  - target f-on representation:  $h \equiv c': \langle a_1, a_2, a_3, a_4, a_5, a_6 \rangle \rightarrow \{0, 1\}$
  - training examples  $D$ : positive and negative examples of target function  $c$
- **Aim:** Find a hypothesis  $h \in H$  such that  $(\forall d \in D) h(d) - c(d) < \varepsilon \approx 0$ , where  $H$  is the set of all possible hypotheses  $h \equiv \langle a_1, a_2, a_3, a_4, a_5, a_6 \rangle$ , where each  $a_k, k = [1..6]$ , may be **'?'** ( $\equiv$  any value is acceptable), **'0'** ( $\equiv$  no value is acceptable), or a specific value.
  - $h \equiv \langle ?, ?, ?, ?, ?, ? \rangle$
  - $h \equiv \langle 0, 0, 0, 0, 0, 0 \rangle$
  - $h \equiv \langle ?, ?, \text{yes}, ?, ?, ? \rangle$

instances

error rate

# Concept Learning as Search

- Concept learning task:
  - target concept: Girls who Simon likes
  - target function:  $c: D \rightarrow \{0, 1\}$
  - data  $d \in D$ : Girls, each described in terms of the following attributes

*instances*

- $a_1 \equiv \text{Hair}$  (possible values: blond, brown, black)
- $a_2 \equiv \text{Body}$  (possible values: thin, average, plump)
- $a_3 \equiv \text{likesSimon}$  (possible values: yes, no)
- $a_4 \equiv \text{Pose}$  (possible values: arrogant, natural, goofy)
- $a_5 \equiv \text{Smile}$  (possible values: none, pleasant, toothy)
- $a_6 \equiv \text{Smart}$  (possible values: yes, no)

$|H| = 1 + 4 \cdot 4 \cdot 3 \cdot 4 \cdot 4 \cdot 3 = 2305$

$h \equiv \langle 0, 0, 0, 0, 0, 0 \rangle$   
*error rate*

target f-on representation:  $h \equiv c': \langle a_1, a_2, a_3, a_4, a_5, a_6 \rangle \rightarrow \{0, 1\}$   
 training examples  $D$ : positive and negative examples of target function  $c$

- **Aim:** Find a hypothesis  $h \in H$  such that  $(\forall d \in D) h(d) - c(d) < \epsilon \approx 0$ , where  $H$  is the set of all possible hypotheses  $h \equiv \langle a_1, a_2, a_3, a_4, a_5, a_6 \rangle$ , where each  $a_k$ ,  $k = [1..6]$ , may be '?' ( $\equiv$  any value is acceptable), '0' ( $\equiv$  no value is acceptable), or a specific value.

*concept learning  $\equiv$  searching through  $H$*

# General-to-Specific Ordering

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- Many concept learning algorithms utilize general-to-specific ordering of hypotheses
- General-to-Specific Ordering:
  - $h1$  precedes (is more general than)  $h2 \Leftrightarrow (\forall d \in D) (h1(d) = 1) \leftarrow (h2(d) = 1)$   
(e.g.,  $h1 \equiv \langle ?, ?, yes, ?, ?, ? \rangle$  and  $h2 \equiv \langle ?, ?, yes, ?, ?, yes \rangle \Rightarrow h1 >_g h2$  )
  - $h1$  and  $h2$  are of equal generality  $\Leftrightarrow (\exists d \in D) \{ [(h1(d) = 1) \rightarrow (h2(d) = 1)] \wedge [(h2(d) = 1) \rightarrow (h1(d) = 1)] \wedge h1 \text{ and } h2 \text{ have equal number of '?' } \}$   
(e.g.,  $h1 \equiv \langle ?, ?, yes, ?, ?, ? \rangle$  and  $h2 \equiv \langle ?, ?, ?, ?, ?, yes \rangle \Rightarrow h1 =_g h2$  )
  - $h2$  succeeds (is more specific than)  $h1 \Leftrightarrow (\forall d \in D) (h1(d) = 1) \leftarrow (h2(d) = 1)$   
(e.g.,  $h1 \equiv \langle ?, ?, yes, ?, ?, ? \rangle$  and  $h2 \equiv \langle ?, ?, yes, ?, ?, yes \rangle \Rightarrow h2 \not>_g h1$  )

# Find-S Algorithm – Example

1. Initialise  $h \in H$  to the most specific hypothesis:  $h \leftarrow \langle a_1, \dots, a_n \rangle$ ,  $(\forall i) a_i = 0$ .
2. FOR each positive training instance  $d \in D$ , do:
  - FOR each attribute  $a_i$ ,  $i = [1..n]$ , in  $h$ , do:
    - IF  $a_i$  is satisfied by  $d$
    - THEN do nothing
    - ELSE replace  $a_i$  in  $h$  so that the resulting  $h' >_g h$ ,  $h \leftarrow h'$ .
3. Output hypothesis  $h$ .

	$c(d)$	$hair$	$body$	$likesSimon$	$pose$	$smile$	$smart$
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

$h \leftarrow \langle 0, 0, 0, 0, 0, 0 \rangle \rightarrow h \equiv d1 \rightarrow h \leftarrow \langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle$

# Find-S Algorithm

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- Find-S is guaranteed to output the most specific hypothesis  $h$  that best fits positive training examples.
- The hypothesis  $h$  returned by Find-S will also fit negative examples as long as training examples are correct.
- However,
  - Find-S is sensitive to noise that is (almost always) present in training examples.
  - there is no guarantee that  $h$  returned by Find-S is the *only*  $h$  that fits the data.
  - several maximally specific hypotheses may exist that fits the data but, Find-S will output only one.
  - Why we should prefer most specific hypotheses over, e.g., most general hypotheses?

# Find-S Algorithm – Example

1. Initialise  $h \in H$  to the most specific hypothesis:  $h \leftarrow \langle a_1, \dots, a_n \rangle, (\forall i) a_i = 0$ .
2. FOR each positive training instance  $d \in D$ , do:
  - FOR each attribute  $a_i, i = [1..n]$ , in  $h$ , do:
    - IF  $a_i$  is satisfied by  $d$
    - THEN do nothing
    - ELSE replace  $a_i$  in  $h$  so that the resulting  $h' >_g h, h \leftarrow h'$ .
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	$c(d)$	$hair$	$body$	$likesSimon$	$pose$	$smile$	$smart$
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3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

Find-S  $\rightarrow h = \langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle$  BUT  $h_2 = \langle \text{blond}, ?, ?, ?, ?, \text{no} \rangle$  fits  $D$  as well

# Find-S Algorithm – Example

1. Initialise  $h \in H$  to the most specific hypothesis:  $h \leftarrow \langle a_1, \dots, a_n \rangle, (\forall i) a_i = 0$ .
2. FOR each positive training instance  $d \in D$ , do:
  - FOR each attribute  $a_i, i = [1..n]$ , in  $h$ , do:
    - IF  $a_i$  is satisfied by  $d$
    - THEN do nothing
    - ELSE replace  $a_i$  in  $h$  so that the resulting  $h' >_g h, h \leftarrow h'$ .
3. Output hypothesis  $h$ .

	$c(d)$	$hair$	$body$	$likesSimon$	$pose$	$smile$	$smart$
1	1	blond	thin	yes	arrogant	toothy	no
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3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

Find-S  $\rightarrow h_1 = \langle blond, ?, ?, ?, no \rangle$  YET  $h_2 = \langle blond, ?, yes, ?, ?, ? \rangle$  fits  $D$  as well

# Candidate-Elimination Algorithm

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- Find-S is guaranteed to output the most specific hypothesis  $h$  that best fits positive training examples.
- The hypothesis  $h$  returned by Find-S will also fit negative examples as long as training examples are correct.
- However,
  1. Find-S is sensitive to noise that is (almost always) present in training examples.
  2. there is no guarantee that  $h$  returned by Find-S is the *only*  $h$  that fits the data.
  3. several maximally specific hypotheses may exist that fits the data but, Find-S will output only one.
  4. Why we should prefer most specific hypotheses over, e.g., most general hypotheses?

To address the last three drawbacks of Find-S, Candidate-Elimination was proposed

# Candidate-Elimination (C-E) Algorithm

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- Main idea: Output a set of hypothesis  $VS \subseteq H$  that fit (are consistent) with data  $D$
- Candidate-Elimination (C-E) Algorithm is based upon:
  - general-to-specific ordering of hypotheses
  - *Def:*  $h$  is consistent (fits) data  $D \Leftrightarrow (\forall \langle d, c(d) \rangle) h(d) = c(d)$
  - *Def:* version space  $VS \subseteq H$  is set of all  $h \in H$  that are consistent with  $D$
- C-E algorithm defines VS in terms of two boundaries:
  - general boundary  $G \subseteq VS$  is a set of all  $h \in VS$  that are the most general
  - specific boundary  $S \subseteq VS$  is a set of all  $h \in VS$  that are the most specific

# Candidate-Elimination (C-E) Algorithm

1. Initialise  $G \subseteq VS$  to the most general hypothesis:  $h \leftarrow \langle a_1, \dots, a_n \rangle, (\forall i) a_i = ?$ .  
Initialise  $S \subseteq VS$  to the most specific hypothesis:  $h \leftarrow \langle a_1, \dots, a_n \rangle, (\forall i) a_i = 0$ .
2. FOR each training instance  $d \in D$ , do:
  - IF  $d$  is a positive example
    - Remove from  $G$  all  $h$  that are not consistent with  $d$ .
    - FOR each hypothesis  $s \in S$  that is not consistent with  $d$ , do:
      - replace  $s$  with all  $h$  that are consistent with  $d$ ,  $h >_g s$ ,  $h \not>_g g \in G$ ,
      - remove from  $S$  all  $s$  being more general than other  $s$  in  $S$ .
  - IF  $d$  is a negative example
    - Remove from  $S$  all  $h$  that are not consistent with  $d$ .
    - FOR each hypothesis  $g \in G$  that is not consistent with  $d$ , do:
      - replace  $g$  with all  $h$  that are consistent with  $d$ ,  $g >_g h$ ,  $h >_g s \in S$ ,
      - remove from  $G$  all  $g$  being less general than other  $g$  in  $G$ .
3. Output hypothesis  $G$  and  $S$ .

# C-E Algorithm – Example

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	<i>c(d)</i>	<i>hair</i>	<i>body</i>	<i>likesSimon</i>	<i>pose</i>	<i>smile</i>	<i>smart</i>
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

$G_0 \leftarrow \{ \langle ?, ?, ?, ?, ?, ? \rangle \}$  ,  $S_0 \leftarrow \{ \langle 0, 0, 0, 0, 0, 0 \rangle \}$

# C-E Algorithm – Example

	<i>c(d)</i>	<i>hair</i>	<i>body</i>	<i>likesSimon</i>	<i>pose</i>	<i>smile</i>	<i>smart</i>
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

*d1 is positive* → *refine S*

*no g* ∈ *G*<sub>0</sub> *is inconsistent with d1* → *G*<sub>1</sub> ← *G*<sub>0</sub> ≡ {⟨?, ?, ?, ?, ?, ?⟩}

*add to S all minimal generalizations of s* ∈ *S*<sub>0</sub> *such that s* ∈ *S*<sub>1</sub> *is consistent with d1*

*S*<sub>1</sub> ← {⟨blond, thin, yes, arrogant, toothy, no⟩}

# C-E Algorithm – Example

	$c(d)$	$hair$	$body$	$likesSimon$	$pose$	$smile$	$smart$
1	1	blond	thin	yes	arrogant	toothy	no
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3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

$d2$  is negative  $\rightarrow$  refine  $G$

no  $s \in S_1$  is inconsistent with  $d2 \rightarrow S_2 \leftarrow S_1 \equiv \{\langle blond, thin, yes, arrogant, toothy, no \rangle\}$

add to  $G$  all minimal specializations of  $g \in G_1$  such that  $g \in G_2$  is consistent with  $d2$

$G_1 \equiv \{\langle ?, ?, ?, ?, ?, ? \rangle\}$

$G_2 \leftarrow \{\langle blond, ?, ?, ?, ?, ? \rangle, \langle ?, ?, yes, ?, ?, ? \rangle, \langle ?, ?, ?, arrogant, ?, ? \rangle, \langle ?, ?, ?, ?, toothy, ? \rangle, \langle ?, ?, ?, ?, ?, no \rangle\}$

# C-E Algorithm – Example

	$c(d)$	<i>hair</i>	<i>body</i>	<i>likesSimon</i>	<i>pose</i>	<i>smile</i>	<i>smart</i>
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

$d_3$  is positive  $\rightarrow$  refine  $S$

two  $g \in G_2$  are inconsistent with  $d_3$ , i.e.,  $\langle ?, ?, ?, arrogant, ?, ? \rangle$  and  $\langle ?, ?, ?, ?, toothy, ? \rangle \rightarrow$   
 $G_3 \leftarrow \{ \langle blond, ?, ?, ?, ?, ? \rangle, \langle ?, ?, yes, ?, ?, ? \rangle, \langle ?, ?, ?, ?, ?, no \rangle \}$

add to  $S$  all minimal generalizations of  $s \in S_2$  such that  $s \in S_3$  is consistent with  $d_3$

$S_2 \equiv \{ \langle blond, thin, yes, arrogant, toothy, no \rangle \}$

$S_3 \leftarrow \{ \langle blond, ?, yes, ?, ?, no \rangle \}$

# C-E Algorithm – Example

	$c(d)$	<i>hair</i>	<i>body</i>	<i>likesSimon</i>	<i>pose</i>	<i>smile</i>	<i>smart</i>
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

$d4$  is negative  $\rightarrow$  refine  $G$

no  $s \in S_3$  is inconsistent with  $d4 \rightarrow S_4 \leftarrow S_3 \equiv \{\langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle\}$

add to  $G$  all minimal specializations of  $g \in G_3$  such that  $g \in G_4$  is consistent with  $d4$

$G_3 \equiv \{\langle \text{blond}, ?, ?, ?, ?, ? \rangle, \langle ?, ?, \text{yes}, ?, ?, ? \rangle, \langle ?, ?, ?, ?, ?, \text{no} \rangle\}$

$G_4 \leftarrow \{\langle \text{blond}, ?, ?, ?, ?, ? \rangle, \langle ?, ?, \text{yes}, ?, ?, ? \rangle\}$

# C-E Algorithm – Example

	$c(d)$	$hair$	$body$	$likesSimon$	$pose$	$smile$	$smart$
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

$d5$  is negative  $\rightarrow$  refine  $G$

no  $s \in S_4$  is inconsistent with  $d4 \rightarrow S_5 \leftarrow S_4 \equiv \{\langle blond, ?, yes, ?, ?, no \rangle\}$

add to  $G$  all minimal specializations of  $g \in G_4$  such that  $g \in G_5$  is consistent with  $d5$

One  $g \in G_4$  is inconsistent with  $d5$ , i.e.,  $\langle blond, ?, ?, ?, ?, ? \rangle \rightarrow$

$G_4 \equiv \{\langle blond, ? \times, ?, ?, ? \rangle, \langle ?, ?, yes, ?, ?, ? \rangle\}$

$G_5 \leftarrow \{\langle ?, ?, yes, ?, ?, ? \rangle\}$

# C-E Algorithm – Example

	$c(d)$	<i>hair</i>	<i>body</i>	<i>likesSimon</i>	<i>pose</i>	<i>smile</i>	<i>smart</i>
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

*Output of C-E:*

*version space of hypotheses  $VS \subseteq H$  bound with  
specific boundary  $S \equiv \{\langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle\}$  and  
general boundary  $G \equiv \{\langle ?, ?, \text{yes}, ?, ?, ? \rangle\}$*

*Output of Find-S:*

*most specific hypothesis  $h \equiv \langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle$*

# C-E Algorithm – Example

	$c(d)$	<i>hair</i>	<i>body</i>	<i>likesSimon</i>	<i>pose</i>	<i>smile</i>	<i>smart</i>
1	1	blond	thin	yes	arrogant	toothy	no
2	0	brown	thin	no	natural	pleasant	yes
3	1	blond	plump	yes	goofy	pleasant	no
4	0	black	thin	no	arrogant	none	no
5	0	blond	plump	no	natural	toothy	yes

*Output of C-E:*

*version space of hypotheses  $VS \subseteq H$  bound with specific boundary  $S \equiv \{\langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle\}$  and general boundary  $G \equiv \{\langle ?, ?, \text{yes}, ?, ?, ? \rangle\}$*

*$VS \equiv \{\langle ?, ?, \text{yes}, ?, ?, ? \rangle, \langle \text{blond}, ?, \text{yes}, ?, ?, ? \rangle, \langle ?, ?, \text{yes}, ?, ?, \text{no} \rangle, \langle \text{blond}, ?, \text{yes}, ?, ?, \text{no} \rangle\}$*



# Concept Learning – Lecture Overview

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- Why machine learning?
- Well-posed learning problems
- Designing a machine learning system
- Concept learning task
- Concept learning as Search
- Find-S algorithm
- Candidate-Elimination algorithm

# Concept Learning – Practice

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- Tom Mitchell's book – chapter 1 and chapter 2
- Relevant exercises from chapter 1: 1.1, 1.2, 1.3, 1.5
- Relevant exercises from chapter 2: 2.1, 2.2, 2.3, 2.4, 2.5

# Course 395: Machine Learning – Lectures

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- Lecture 1-2: Concept Learning
- Lecture 3-4: Decision Trees & CBC Intro
- Lecture 5-6: Evaluating Hypotheses
- Lecture 7-8: Artificial Neural Networks I
- Lecture 9-10: Artificial Neural Networks II
- Lecture 11-12: Artificial Neural Networks III
- Lecture 13-14: Instance Based Learning & Genetic Algorithms